Common Mistakes in Modelling

• Mistake: **No Primary Key**
  – Just don’t do that outside of simple examples
  – (same is true for cardinalities)

• Mistake: **No Relation Symbol or Name**

• Mistake: **Modelling Functionality as Data**
  – “Users can write reviews for a book, which they can also delete.”
Mistake: **Primary Key does not make sense**

- **Intuition:** An attribute / set of attributes which uniquely identify an entity
- **Additional soft constraints**
  - Should feel “natural”
  - Should be minimal
  - Should be easy to handle
- **Example: Modeling a book in a book store**
  - **Good:** Book(name, author, year, isbn, summary, price)
  - **Less good:** Book(name, author, year, isbn, summary, price)
    - More natural, but more complex. Only valid if it is guaranteed that a given author writes only a single book with the same name in a year. Depends on task if this makes sense.
  - **Not good or even invalid:**
    - Book(name, author, year, isbn, summary, price)
    - Book(name, author, year, isbn, summary, price)
- **Weak Entities always have composite key**
  - One component is the primary key of the strong entity, the second component is with the weak entity and is only unique within the set of weak entities belonging to the same strong one
• **Mistake: Confusing Cardinality Notations**
  – **Warning:** There are several conflicting ways of writing cardinalities!
    • Whichever way you choose, **BE CONSISTENT**!
  – **Classic ER Style (default in this lecture):**
    • Read cardinalities in diagram below as
      – “each entity of *woman* participates in any number of relationships of *mother_of*, while each entity in *child* must participate in exactly one”
    • This notation is needed for non-trivial n-ary relationships (n>2)
– **UML Style** (not our lecture’s default):

  • Read cardinalities in diagram below as
    – “each one entity of *woman* is in relation (via *mother_of*) with any number of entities of *child*”
  • Usually only distinguishes between 0, 0..1, 1, 0..* and *
    – Fine-granular cardinalities and higher arity relations not easily possible

![Diagram showing relationships between Woman, mother_of, and Child]
Mistake: **Model not suitable for the task**

- Task: “Build a person database. Each person should have a mother and a father. The database should be used to explore ancestry.”
- Very Bad
- Still quite Bad:
Common Mistakes in Modelling

– Better:

– Or maybe:
5 Relational Model

- Basic Set Theory
- Relational Model
- From Theory to Practice
- Integrity Constraints
- Conversion from ER
5.1 Basic Set Theory

• **Set theory** is the foundation of mathematics
  – you probably all know these things from your math courses, but repeating never hurts
  – the **relational model** is based on set theory; understanding the basic math will help a lot
5.1 Sets

• A set is a mathematical **primitive**, and thus has no formal definition

• A set is a **collection** of objects (called *members* or *elements* of the set)
  – objects (or entities) have to be understood in a very broad sense, can be anything from physical objects, people, abstract concepts, other sets, …

• Objects **belong** (or do **not belong**) to a set (alternatively, *are* or *are not* in the set)

• A set **consists** of all its elements
5.1 Sets

• Sets can be specified **extensionally**
  – list all its elements
  – e.g. \( A = \{ \text{ifis, 42, Balke, Hurz!} \} \)

• Sets can be specified **intensionally**
  – provide a criterion deciding whether an object belongs to the set or not (**membership criterion**)
  – examples:
    • \( A = \{ x \mid x > 4 \text{ and } x \in \mathbb{Z} \} \)
    • \( B = \{ x \in \mathbb{N} \mid x < 7 \} \)
    • \( C = \{ \text{all facts about databases you should know} \} \)

• Sets can be either **finite** or **infinite**
  – set of all super villains is finite
  – set of all numbers is infinite
5.1 Sets

• Sets are different, iff they have different members
  – \{a, b, c\} = \{b, c, a\}
  – duplicates are not supported in standard set theory
    • \{a, a, b, c\} = \{a, b, c\}

• Sets can be empty (written as \{\} or \emptyset)

• Notations for set membership
  – a \in \{a, b, c\}
  – e \notin \{a, b, c\}
5.1 Sets

• Defining a set by its **intension**
  – intension must be **well-defined and unambiguous**
  – there is always is a clear **membership criterion**
    to determine whether an object belongs to the set (or not)

– Example for an invalid definition (Russell’s paradox):

  In a small town, there is just one male barber. He shaves all and only those men in town who do not shave themselves.

  • does the barber shave himself?
5.1 Sets

• Still, the set’s extension might be unknown (however, there is one)

• Example
  – All students in this room who are older than 22.
  – well-defined, but not known to me …
  – but (at least in principle) we can find out!

• Why should we care? Because:
  – Intensional set $\approx$ database query
  – Extensional set $\approx$ result of a query, table
5.1 Sets

• For every set and object, there is an accompanying definition of equality (or equivalence)
  – is \( x = y \)?

• However, you could have two different descriptions of the same element
  – example: the set of all 26 standard letters
    • ‘ö’ is not contained in this set
    • ‘m’ = ‘M’ and both reflect a single element of the set
      – ‘m’ and ‘M’ are different descriptions of the same object
  – example: the set of all 59 letters and umlauts in German
    • ‘ö’ is element of the set
    • ‘m’ ≠ ‘M’ and are both elements of the set (two different objects)
5.1 Sets

• Sets have a cardinality (i.e., number of elements)
  – denoted by $|A|$
  – $|\{a, b, c\}| = 3$

• Set $A$ is a **subset** of set $B$, denoted by $A \subseteq B$, iff every member of $A$ is also a member of $B$

• $B$ is a **superset** of $A$, denoted by $B \supseteq A$, iff $A \subseteq B$
5.1 Tuples

• A **tuple** (or vector) is a sequence of objects
  – length 1: Singleton
  – length 2: Pair
  – length 3: Triple
  – length $n$: $n$-tuple

• In contrast to sets…
  – tuples can contain an object more than once
  – the objects appear in a certain **order**
  – the length of the tuple is **finite**

• Written as $\langle a, b, c \rangle$ or $(a, b, c)$
5.1 Tuples

• Hence
  – \(\langle a, b, c \rangle \neq \langle c, b, a \rangle\), whereas \(\{a, b, c\} = \{c, b, a\}\)
  – \(\langle a_1, a_2 \rangle = \langle b_1, b_2 \rangle\) iff \(a_1 = b_1\) and \(a_2 = b_2\)

• \(n\)-tuples \((n > 1)\) can also be defined as a cascade of ordered pairs:
  – \(\langle a, b, c, d \rangle = \langle a, \langle b, \langle c, d \rangle \rangle \rangle\)
5.1 Set Operations

- **Four binary set operations**
  - union, intersection, difference and cartesian product
- **Union: \( \cup \)**
  - creates a new set containing all elements that are contained in (at least) one of two sets
  - \( \{a, b\} \cup \{b, c\} = \{a, b, c\} \)
- **Intersection: \( \cap \)**
  - creates a new set containing all elements that are contained in both sets
  - \( \{a, b\} \cap \{b, c\} = \{b\} \)
5.1 Set Operations

• Difference: \ 
  – creates a set containing all elements of the first set without those also being in the second set
  – \{a, b\} \ {b, c\} = \{a\}
5.1 Set Operations

• **Cartesian Product: \( \times \)**
  - the cartesian product is an operation between two sets, creating a new set of pairs such that:
    \[
    A \times B = \{ \langle a, b \rangle \mid a \in A \text{ and } b \in B \}\]
  - named after René Descartes

• **Example**
  - \( \{a, b\} \times \{b, c\} = \{\langle a, b \rangle, \langle a, c \rangle, \langle b, b \rangle, \langle b, c \rangle\} \)
  - Cleverness = \{ genius, dumb \}
  - Character = \{ hero, villain \}
  - Cleverness \( \times \) Character = \{\langle genius, hero\rangle, \langle dumb, hero\rangle, \langle genius, villain\rangle, \langle dumb, villain\rangle\}

• The cartesian product can easily be extended to higher dimensionalities: \( A \times B \times C \) is a set of triples
5.1 Relations

- A **relation** $R$ over some sets $D_1, \ldots, D_n$ is a **subset** of their **cartesian product**
  - $R \subseteq D_1 \times \ldots \times D_n$
  - the elements of a relation are **tuples**
  - the $D_i$ are called **domains**
  - each $D_i$ corresponds to an **attribute** of a tuple
    - $n=1$: Unary relation or **property**
    - $n=2$: Binary relation
    - $n=3$: Ternary relation
    - ...
• Some important properties

  – relations are sets in the mathematical sense, thus no duplicate tuples are allowed
  – the set of tuples is unordered
  – the list of domains is ordered
  – relations can be modified by…
    • inserting new tuples,
    • deleting existing tuples, and
    • updating (that is, modifying) existing tuples.
• **A special case: Binary relations**
  
  - \( R \subseteq D_1 \times D_2 \)
    - \( D_1 \) is called **domain**, \( D_2 \) is called **co-domain** (range, target)
  
  - relates objects of two different sets to each other
  
  - \( R \) is just a set of ordered pairs
  
  - \( R = \{\langle a,1 \rangle, \langle c,1 \rangle, \langle d,4 \rangle, \langle e,5 \rangle, \langle e,6 \rangle\} \)
    - can also be written as \( aR1, cR1, dR4, \ldots \)
  
  - imagine **Likes \subseteq Person \times Beverage**
    - Tilo Likes Coffee, Christian Likes Tea, ...
  
  - For example, binary relations can naively be used to implement n:m relationship types in a logical data model
  
  - Functions are a special case of binary relations
5.1 Relations

• Example
  – Accessory = \{spikes, butterfly helmet\}
  – Material = \{silk, armor plates\}
  – Color = \{pink, black\}

\[
\text{Color} \times \text{Material} \times \text{Accessory} = \\
\{\langle \text{pink, silk, butterfly helmet} \rangle, \langle \text{pink, silk, spikes} \rangle, \langle \text{pink, armor plates, butterfly helmet} \rangle, \langle \text{pink, armor plates, spikes} \rangle, \langle \text{black, silk, butterfly helmet} \rangle, \langle \text{black, silk, spikes} \rangle, \langle \text{black, armor plates, butterfly helmet} \rangle, \langle \text{black, armor plates, spikes} \rangle\}
\]
5.1 Relations

• Relation **FamousHeroCostumes** \(\subseteq \text{Color} \times \text{Material} \times \text{Accessory} \)

\[
\text{FamousHeroCostumes} = \{(\text{pink, silk, butterfly helmet}),
(\text{black, armor plates, spikes})\}
\]
5.1 Functions

- **Functions** are special case of binary relations
  - **partial function:**
    each element of the domain is related to
    **at most one** element in the co-domain
  
- **total function:**
  each element in the domain is related to
  **exactly one** element in the co-domain
5.1 Functions

• Functions can be used to abstract from the exact order of domains in a relation
  – alternative definition of relations: a relation is a set of functions
  – every tuple in the relation is considered as a function of the type \( \{A_1, ..., A_n\} \rightarrow D_1 \cup \ldots \cup D_n \)
    • that means, every tuple maps each attribute to some value
5.1 Functions

• Example
  – Color = \{pink, black\}
  – Material = \{silk, armor plates\}
  – Accessory = \{spikes, butterfly helmet\}
  – to be independent of the domain order, the tuple \langle pink, silk, butterfly helmet \rangle can also be represented as the following function \( t \)
    • \( t(\text{Color}) = \text{pink} \)
    • \( t(\text{Material}) = \text{silk} \)
    • \( t(\text{Accessory}) = \text{butterfly helmet} \)
  – Usually, one writes \( t[\text{color}] \) instead of \( t(\text{color}) \)
  – This can be used to change the order of domains for tuples
    • \( t[\text{Material, Accessory, Color}] = \langle \text{silk, butterfly helmet, pink} \rangle \)
5 Relational Model

- Basic Set Theory
- Relational Model
- From Theory to Practice
- Integrity Constraints
- Conversion from ER
• Well, that’s all nice to know… but: we are here to learn about databases!
  – where is the connection?

• Here it is…
  – a database schema is a description of concepts in terms of relations and attribute domains
  – a database instance is a set of tuples having certain attribute values
5.2 Relational Model

• OK, then…
  – designing a database schema (e.g., by ER modeling) determines entities and relationships, as well as their corresponding sets of attributes and associated domains
  – the Cartesian product of the respective domains is the set of all possible instances (of each entity type or relationship type)
  – a relation formalizes the actually existing subset of all possible instances
5.2 Relational Model

- Database schemas are described by relation schemas $R(A_1, \ldots, A_n)$
- Domains are assigned by the $\text{dom}$ function
  - $\text{dom}(A_1) = D_1$, $\text{dom}(A_2) = D_2$, ...
  - Also written as: $R(A_1:D_1, \ldots, A_n:D_n)$
- The actual database instance is given by a set of matching relations
- Example
  - relation schema: $\text{Cat(name: string, age: number)}$
  - A matching relation: \{(Blackie, 2), (Kitty, 1), (Fluffy, 4)\}
5.2 Relational Model

- Relations can be written as **tables**

<table>
<thead>
<tr>
<th>PERSON</th>
<th>first name</th>
<th>last name</th>
<th>sex</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clark Joseph</td>
<td>Kent</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td>Louise</td>
<td>Lane</td>
<td>f</td>
<td></td>
</tr>
<tr>
<td>Lex</td>
<td>Luthor</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td>Charles</td>
<td>Xavier</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td>Erik</td>
<td>Magnus</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td>Jeanne</td>
<td>Gray</td>
<td>f</td>
<td></td>
</tr>
<tr>
<td>Ororo</td>
<td>Munroe</td>
<td>f</td>
<td></td>
</tr>
<tr>
<td>Tony Edward</td>
<td>Stark</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td>Matt</td>
<td>Murdock</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td>Raven</td>
<td>Wagner</td>
<td>f</td>
<td></td>
</tr>
<tr>
<td>Robert Bruce</td>
<td>Banner</td>
<td>m</td>
<td></td>
</tr>
</tbody>
</table>
5.2 Relational Model

• A **relational database schema** consists of
  – a set of relation schemas
  – a set of integrity constraints

• A **relational database instance** (or state) is
  – a set of relations adhering to the respective schemas
  and respecting all integrity constraints
Every relational DBMS needs a language to define its relation schemas (and integrity constraints)

– **Data Definition Language** (DDL)
– typically, it is difficult to formalize all possible integrity constraints, since they tend to be complex and vague

A relational DBMS also needs a language to handle and manipulate tuples

– **Data Manipulation Language** (DML)

Today’s RDBMS use **SQL** as both DDL and DML

– Compare to XML: Here, DDL and DML are separated
5 Relational Model

- Basic Set Theory
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- Conversion from ER
In the early 1970s, the relational model became a hot topic in database research. Based on set theory, a relation is a subset of the cartesian product over a list of domains.

Early query interfaces for the relational model:
- Relational Algebra
- Tuple Relational Calculus (SQUARE, SEQUEL)
- Domain Relational Calculus (QBE)

Question: How to build a working database management system using this theory?
5.3 From Theory to Practice

• **System R** was the first working prototype of a relational database system (starting 1973)
  – most **design decisions** taken during the development of System R substantially **influenced** the design of **subsequent systems**

• **Questions**
  – how to store and represent data?
  – how to query for data?
  – how to manipulate data?
  – how do you do all this with good performance?
The challenge of the **System R** project was to create a working prototype system

- theory is good
- but developers were willing to sacrifice theoretical beauty and clarity for the sake of usability and performance

**Vocabulary change**

- mathematical terms were too unfamiliar for most people
- *table* = relation
- *row* = tuple
- *column* = attribute
- *data type, domain* = *domain*
• **Design decisions:**
  During the development of System R, two major and very controversial decisions had been made
  – allow duplicate tuples
  – allow **NULL** values
• Those decisions are still subject to discussions…
• Duplicates

  – in a relation, there cannot be any duplicate tuples
  – also, query results cannot contain duplicates

  • the relational algebra and relational calculi all have implicit duplicate elimination
Practical considerations

- you want to query for **name** and **birth year** of all **students** of TU Braunschweig
- the result returns roughly **20,000 tuples**
- probably there are **some** duplicates
- it’s **1973**, and your computer has **16 kilobytes** of main memory and a very slow external storage device...
- to eliminate duplicates, you need to **store** the result, **sort** it, and **scan** for adjacent duplicate lines

  - System R engineers concluded that this effort is not worth the effect
  - duplicate elimination in result sets happens only on-request
• **Decision:** Don’t eliminate duplicates in results
• **What about the tables?**
  – again: ensuring that no duplicates end up in the tables requires some work
  – engineers also concluded that there is actually no need in enforcing the no-duplicate policy
    • if the user wants duplicates and is willing to deal with all the arising problems – then that’s fine

• **Decision:** Allow duplicates in tables
• As a result, the theory underlying relational databases shifted from *set theory* to *multi-set theory*
  – straightforward, only notation is more complicated
• Sometimes, an attribute value is not known or an attribute does not apply for an entity
  – e.g. what value should the attribute `university_degree` take for the entity Heinz Müller, if Heinz Müller does not have any degree?
  – e.g. you regularly observe the weather and store temperature, wind strength, and air pressure every hour – and then your barometer breaks... what now?
• Possible solution: For each domain, define a value indicating that data is not available, not known, not applicable, …
  
  – for example, use none for Heinz Müller’s degree, use −1 for missing pressure data, …

  – Problem:
    • you need such a special value for each domain or use case
    • you need special failure handling for queries, e.g. compute average of all pressure values that are not −1
5.3 From Theory to Practice

• Again, system designers chose the simplest solution (regarding implementation): **NULL values**
  
  – **NULL** is a special value which is usable in any domain and represents that data is just not there
    
    • there are many interpretations of what NULL actually means
  
  – Systems have some default rules how to deal with NULL values
    
    • aggregation functions usually ignore rows with NULL values (which is good in most, but not all cases)
    
    • three-valued logic
    
    • however, creates some strange anomalies
Another tricky problem: How should users query the DB?

Classical answer

- Relational Algebra and Relational Calculi
- problem: more and more non-expert users

More natural query interfaces:

- QBE (query by example)
- SEQUEL (structured English query language)
- SQL: the current standard; derived from SEQUEL
5 Relational Model

- Basic Set Theory
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5.4 Integrity Constraints

• Integrity constraints are difficult to model in ER
  – basically annotations to the diagram, especially for behavioral constraints
    • e.g. The popularity rating of any sidekick should always be less than the respective super hero’s.

• But some structural constraints can directly be expressed
  – e.g., key constraints, functionalities
  – Formally, they are not part of the mathematical model, we still integrate them for practical purposes
5.4 Basic Constraints

• Primary Key Constraint
  – A relation is defined as a set of tuples
    • all tuples have to be distinct, i.e., no two tuples can have the same combinations of values for all attributes
    • so-called uniqueness (unique key) constraint or primary key constraint
  – Therefore, we can define the key of a relation as a designated subset of attributes for which no two tuples have the same values (are unique)
    • It‘s a little bit more complex than that…see lecture 10
  – Each relation will need a designated key
    • We will write this as for example Hero(alias, name, age, ...)
5.4 Basic Constraints

• **NOT NULL Constraint**
  
  -- Remember, a relation is defined as \( R \subseteq D_1 \times \ldots \times D_n \) with tuples \( t \in R \)
  
  -- However, in a practical application it's common that not always all attribute values are known
  
  • Therefore, it is usually assumed that there is a special NULL value in each domain, i.e. \( NULL \in D_i \)
  
  -- Sometimes, this is not desired for certain attributes
  
  • Introduces the **NOT NULL constraint**
  
  -- **Primary Key must never be NULL**
  
  -- e.g. Address(  
    street: string NOT NULL,  
    number: numeric NOT NULL,  
    zip-code: numeric NOT NULL,  
    city: string NOT NULL  
    postbox: string)
5.4 Basic Constraints

- **Foreign Key Constraint**
  - Sometimes, we want to link tuples in different relations
    - This will be integral for realizing ER relationships in a database
  - A **foreign key constraint** can be defined between the key attributes of one relation and some attributes of another one
    - e.g., `Hero(id, first name, last name)`
    - `Aliases(alias, heroid→Hero)`
  - Tuples of the referring relation can only have values for the referencing attribute which are the key of an existing tuple in the referenced relation
    - This is called **referential integrity**
5.4 Basic Constraints

Example:

Hero(id, first name, last name)
Aliases(alias, heroid→Hero)

<table>
<thead>
<tr>
<th>Hero</th>
<th>id</th>
<th>firstname</th>
<th>lastname</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1</td>
<td>Charles</td>
<td>Xaviar</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>James</td>
<td>Howlett</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>Jean</td>
<td>Grey</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>Max</td>
<td>Eisenhardt</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Aliases</th>
<th>alias</th>
<th>heroid</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Logan</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>Wolverine</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>Weapon X</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>Eric Magnus</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>Magneto</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>Professor X</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>White Queen</td>
<td>5</td>
</tr>
</tbody>
</table>

Invalid!
• Convention:
  – If a composite key is referenced, we write this as, e.g.,
    \( R_1(a, b, c) \quad R_2(d, e, f, (d, f) \rightarrow R_1) \)
  – This is not a standard notation, but rather close to
    what you find in SQL.
5.4 First Normal Form

• There is another major \textit{constraint} on the attributes’ data types in the relational model – the value of any attribute must be \textit{atomic}, that is, it \textbf{cannot be composed} of several other attributes

  • if this property is met, the relation is often referred to as a being in \textbf{first normal form} (1NF or minimal form)
  • in particular, \textit{set-valued} and relation-valued attributes (tables within tables) are \textbf{prohibited}
5.4 First Normal Form

• Example of a **set-valued** column
  – *A person may own several telephones (home, office, cell, …).*

<table>
<thead>
<tr>
<th>Person</th>
<th>first name</th>
<th>last name</th>
<th>telephone no</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clark</td>
<td>Joseph</td>
<td>Kent</td>
<td>5555678</td>
</tr>
<tr>
<td>Louise</td>
<td>Lane</td>
<td></td>
<td>{3914533, 3556576, 5463456}</td>
</tr>
<tr>
<td>Lex</td>
<td>Luthor</td>
<td></td>
<td>4543689</td>
</tr>
<tr>
<td>Charles</td>
<td>Xavier</td>
<td></td>
<td>7658736</td>
</tr>
<tr>
<td>Erik</td>
<td>Magnus</td>
<td></td>
<td>{1252345, 8766781}</td>
</tr>
</tbody>
</table>
5.4 First Normal Form

• Please note, it is possible to model composed attributes in ER models…

• To transform such a model into the relational model, a normalization step is needed
  – this is not always trivial, e.g., what happens to keys?

<table>
<thead>
<tr>
<th>Person</th>
<th>first_name</th>
<th>last_name</th>
<th>telephone_no</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clark Joseph</td>
<td>Joseph</td>
<td>Kent</td>
<td>555-5678</td>
</tr>
<tr>
<td>Louise</td>
<td></td>
<td>Lane</td>
<td>391-4533</td>
</tr>
<tr>
<td>Louise</td>
<td></td>
<td>Lane</td>
<td>355-6576</td>
</tr>
<tr>
<td>Louise</td>
<td></td>
<td>Lane</td>
<td>546-3456</td>
</tr>
<tr>
<td>Lex</td>
<td></td>
<td>Luthor</td>
<td>454-3689</td>
</tr>
<tr>
<td>Charles</td>
<td></td>
<td>Xavier</td>
<td>765-8736</td>
</tr>
<tr>
<td>Erik</td>
<td></td>
<td>Magnus</td>
<td>125-2345</td>
</tr>
<tr>
<td>Erik</td>
<td></td>
<td>Magnus</td>
<td>876-6781</td>
</tr>
</tbody>
</table>
5.4 First Normal Form

• In a purely relational database, all relations are in first normal form
  
  – **object-oriented** databases feature multi-valued attributes, thus closing the modeling gap
  
  – **object-relational extensions** integrate user-defined types (UDTs) into relational databases
    
    • Oracle from version 9i, IBM DB2 from version 8.1, …
5 Relational Model

- Basic Set Theory
- Relational Model
- From Theory to Practice
- Integrity Constraints
- Conversion from ER
After modeling a conceptual schema (e.g., using an ER diagram), the schema can be (semi-) automatically transformed into a relational schema.
The ER diagram is **semantically richer** than the relational model

- However, it's not a real subset

Many constraints are very hard/impossible to express
- disjoint/overlapping generalization
- non-trivial cardinalities – like (1,20), (3,3) or even (1,*)
- ...

Therefore, it usually is a really good idea to create an ER diagram before coding a logical schema
• Question: How to convert EER to relation?
  – We can automatically convert a conceptual ER model to relations
    • Some heuristics follow…
    • However, quite often the result will not be as desired
    • Therefore, still some manual optimization and steering is beneficial
    • While designing a model, it might be very beneficial to keep the result relations and the desired queries in mind…
5.5 Conversion from ER

- Converting a simple Entity Type into a relation schema:

\[ \text{Hero}(\text{id}, \text{name}, \text{alias}) \]
5.5 Conversion from ER

- Converting an n:m relationship type into a relation schema:
  - Relationship type becomes a separate relation schema
  - Links entities of the respective types by using their foreign keys

\[
\text{Hero}(id, \text{name}, \text{alias})
\]

\[
\text{Villain}(id, \text{name}, \text{alias})
\]

\[
\text{hero}_\text{fights}_\text{villain}(\text{hero} \rightarrow \text{Hero}, \text{villain} \rightarrow \text{Villain})
\]
5.5 Conversion from ER

• Converting an 1:m relationship type a relation schema:
  – Entity Type at 1-side can only participate once at the relationship type
    => Push relationship type to the 1-side

Villain(id, name, alias)

Lair(coordinates, awesomeness, owner→Villain)
5.5 Conversion from ER

- Converting an 1:1 relationship type a relation schema:
  - A little bit tricky...
    - Cannot be expressed just by the relation schemas...
    - Just choose one side as the 1-side and implement it just like a 1:m relationship type

```
Hero(id, name, alias)
```

```
Sidekick(id, name, alias, supervisor \rightarrow Hero)
```

- To check if it really 1:1 we need advanced constraints
  - e.g. by using triggers (to be introduced in lecture 14)
How to deal with attributes attached to the rel. type
– Put them wherever you put the respective foreign key(s)

Scientist(id, name, #lab_coats)
Invention(id, code_name)

scientist_works_on_invention(
    scientist → Scientist,
    invention → Invention,
    hours
)
What about n-ary relationship types? (n>2)

– Just apply the exact same approaches:

```
sc_wrk_on_inv_in_lab(
  scientist → Scientist,
  invention → Invention,
  lab → Lab
  hours)
```
5.5 Conversion from ER

- Converting a weak entity into a relation schema:
  - Weak entities are only unique together with the entity at the identifying relationship
  => Follow ident. rel. and inherit respective foreign keys

\[
\text{Evil\_Plan}(\text{code\_name, chance\_of\_success})
\]

\[
\text{todo\_item}(\text{priority\_order, evil\_plan} \rightarrow \text{Evil\_Plan, done})
\]
• How to deal with multi-attributes and composite attributes
  – **composition**: just flatten it
  – **multi-attribute**: treat it like a weak entity

```sql
Secret_Hideout(id, addr_city, addr_street, addr_number)
hideout_name (hideout → Secret_Hideout, name)
```
Converting types with inherited attributes/relations into a relation schema:

- Can be implemented in many ways (depending on inheritance type)
- **Most generic way:** Inherit foreign keys from super type

<table>
<thead>
<tr>
<th>Gadget(id, name)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weapon(gadget → Gadget, range)</td>
</tr>
<tr>
<td>Util_gadget(gadget → Gadget, weight)</td>
</tr>
</tbody>
</table>
• Example:

```
5.5 Conversion from ER
```

```
<table>
<thead>
<tr>
<th>Class</th>
<th>Attributes &amp; Cardinality</th>
</tr>
</thead>
<tbody>
<tr>
<td>Person</td>
<td>surname, firstname, lastname</td>
</tr>
<tr>
<td>Hero</td>
<td>weakness, alias</td>
</tr>
<tr>
<td>Power</td>
<td>name, description, solution</td>
</tr>
<tr>
<td>Side Effect</td>
<td>type, reach, name, description, solution</td>
</tr>
</tbody>
</table>

```

The diagram shows the relationships between the classes and their attributes, along with the cardinality of each relationship. The relationships are as follows:

- Person has one to many Hero
- Hero has one to many Power
- Power has one to many Side Effect
5.5 Conversion from ER

- Entity types:

```plaintext
Hero(firstname: string, lastname: string, alias: string, weakness: string, telephone_no: string)

Person(firstname: string, lastname: string)

(Person(firstname, lastname) → Person

(phone no: string)

firstname

lastname

alias

weakness

Person

Hero
```
5.5 Conversion from ER

- Relationship types: N:M

**Power**
- `name`: string,
- `type`: string,
- `reach`: numeric

**Uses**
- `firstname`: string,
- `lastname`: string,
- `name`: string → Power,
- `situation`: string,
- `(firstname, lastname) → Hero`
5.5 Conversion from ER

- Relationship types: 1:N

**Power**(name: string, type: string, reach: numeric)

**SideEffect**(description: string, power: string → Power, solution: string)
• Relational Algebra
  – Basic relational algebra operations
  – Additional derived operations
• Query Optimization
• Advanced relational algebra
  – Outer Joins
  – Aggregation