

## Deductive Databases & Knowledge Based Systems

### Sheet I

This exercise is completely optional. If you want any corrections, feel free to hand in your solutions on **paper** into the mailbox at the IFIS floor (Mühlenpfordtstraße 23, 2<sup>nd</sup> floor, opposite of elevator). You may answer in either German or English.

#### Exercise 1 (17 points)

All the sub-exercises should be answered with First Order Logic in mind. Answer briefly!

1. Describe the relation between a **language**, an **interpretation**, and a **system**. (3 points)
2. What is the difference between **functions** and **predicates**? Could you use functions instead of predicates or vice-versa? (3 points)
3. What is the difference between a **term** and an **atom**? (2 points)
4. What is an **open** or **closed** formula? (2 points)
5. What is a **rectified formula** and which problem does it address? (2 points)
6. What is the difference between an interpretation and a substitution? Would it be a good idea to merge the **substitution** into the **interpretation**? (3 points)
7. What is **closed world assumption** and why is it often used in deductive databases? (2 points)

#### Exercise 2 (16 points)

All the sub-exercises should be answered with First Order Logic in mind.

1. Design a first order **language** for simple arithmetic's on natural numbers. One should be able to add numbers, subtract numbers, multiply two numbers, decide if a number is equal another number, and if a number is greater than another number. (4 points)
2. Provide an **interpretation** for your language of the previous sub-exercise. (4 points)
3. Provide a formula for following statements: (4 points)
  - a. "5 is greater than 2"
  - b. "If x is greater than 0, then also  $x*y$  is greater than 0"
  - c. "x is either greater than y, or x is equal to y, or x is smaller than y"
  - d. "The sum of any two numbers is always smaller than the product of the same two numbers"

4. Evaluate the previous terms a-d. Are they always true? Can they be true?  
If a term is not always true but can be true, provide an example substitution which makes it true. (4 points)

### Exercise 3 (8 points)

All the sub-exercises should be answered with First Order Logic in mind.

1. Given is a language  $\mathcal{L} = (\Gamma, \Omega, \Pi, X)$  with  $\Gamma := \{a, b\}$ ,  $\Omega := \{f(x), g(x, y)\}$ ,  $\Pi := \{P, Q(x, y), R(x)\}$ , and  $X := \{x, y\}$ .
  - a. Provide at least 10 (different) terms for  $\mathcal{L}$ . (2 points)
  - b. Provide at least 6 (different) atoms for  $\mathcal{L}$ . (2 points)
2. Are the following “strings” valid formulas with respect to  $\mathcal{L}$ ? (4 points)
  - a.  $f(g(x, y))$
  - b.  $P$
  - c.  $Q(x, y) \vee Q(a, b)$
  - d.  $Q(g(f(a), x), f(y))$
  - e.  $\forall a(R(a))$
  - f.  $\exists x(f(x))$
  - g.  $R(x) \rightarrow \neg R(x)$
  - h.  $\neg R(\neg R(f(x)))$